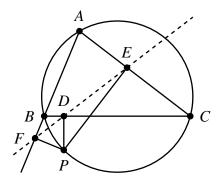
Problem Set #5 MATH 387 : 2015

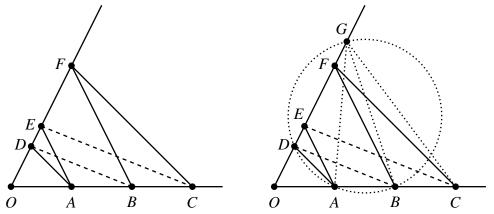
Due: Thursday, 5 February 2015

- 1. Given a line segment AB, construct a regular pentagon having AB as a side.
- **2.** Given a triangle *ABC*, consider a point *P* on its circumscribed circle. Let *D*, *E*, and *F* be the feet of the perpendiculars from the sides of the triangles (extended as necessary) passing through *P*. Prove that the points *D*, *E*, and *F* are collinear.



Hint. Use cyclic quadrilaterals and Eucl.I.14.

3. Consider two lines intersecting at the point *O*. Let *A*, *B*, and *C* be points on the first line and let *D*, *E*, and *F* be points on the second line. If *AD* is parallel to *CF* and *AE* is parallel to *BF*, then prove that *BD* is parallel to *CE*.



Hint. Draw the circle passing through the points *A*, *B*, and *D*. Let *G* be the intersection point between this circle and the second line. Use cyclic quadrilaterals and Eucl.I.29.

Bonus. Complete Levels 13-25 in Euclid: The Game. How many Golden medals can you get?

