# Problem Set \#5 <br> MATH 387: 2015 

Due: Thursday, 5 February 2015

1. Given a line segment $A B$, construct a regular pentagon having $A B$ as a side.
2. Given a triangle $A B C$, consider a point $P$ on its circumscribed circle. Let $D, E$, and $F$ be the feet of the perpendiculars from the sides of the triangles (extended as necessary) passing through $P$. Prove that the points $D, E$, and $F$ are collinear.


Hint. Use cyclic quadrilaterals and Eucl.I.14.
3. Consider two lines intersecting at the point $O$. Let $A, B$, and $C$ be points on the first line and let $D, E$, and $F$ be points on the second line. If $A D$ is parallel to $C F$ and $A E$ is parallel to $B F$, then prove that $B D$ is parallel to $C E$.


Hint. Draw the circle passing through the points $A, B$, and $D$. Let $G$ be the intersection point between this circle and the second line. Use cyclic quadrilaterals and Eucl.I.29.

Bonus. Complete Levels 13-25 in Euclid: The Game. How many Golden medals can you get?

