

# Queen's Algebraic Geometry — Seminar —

## A SOLUTION TO THE WARING PROBLEM FOR MONOMIALS

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### Abstract

The Waring Problem for Polynomials asks: given a homogeneous form  $F$  of degree  $d$  in the polynomial ring  $k[x_0, \dots, x_n]$  where  $k$  an algebraically closed field of characteristic 0, what is the shortest representation of  $F$  as a sum of  $d^{\text{th}}$  powers of linear forms?

The spectacular theorem of Alexander and Hirschowitz, determining the dimensions of the higher Secant Varieties of the Veronese Varieties, answers this question for the *general* form of degree  $d$ . Unfortunately, it is impossible to tell if any given form  $F$  is *general*, in this sense. So, the question has remained open to determine the length of this shortest representation for a given form  $F$ . In this talk, I will explain what the answer is for monomials and indicate other theorems that we have recently proved. This is a report on joint work with E. Carlini and M.V. Catalisano.

Monday 16 January 2012  
15:30 – 16:30  
319 Jeffery Hall